Fast transitions of X-ray variability in the black hole transient GX 339–4: comparison with MAXI J1820+070 and MAXI J1348–630

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ABSTRACT

Fast transitions between different types of power density spectra (PDS) happening over timescales of several tens of seconds are rare phenomena in black hole X-ray binaries. In this paper, we report a broadband spectral-timing analysis of the fast transitions observed in the 2021 outburst of GX 339–4 using *NICER* and *Insight*-HXMT observations. We observe transitions between band-limited noise-dominated PDS and type-B quasi-periodic oscillations (QPOs), and their rapid appearance or disappearance. We also make a detailed comparison between the fast transitions in GX 339–4 with those seen in MAXI J1820+070 and MAXI J1348–630. By comparing the spectra of the periods with and without type-B QPOs, we find that the spectral ratios above 10 keV are nearly constant or slightly decreasing, and the values are different between sources. Below 10 keV, the flux change of the Comptonization component is inversely proportional to the flux change of the thermal component, suggesting that the appearance of type-B QPOs is associated with a redistribution of the accretion power between the disc and the Comptonizing emission region. The spectral ratios between the periods with type-B QPO and those with broadband noise are significantly different from that with type-B QPO and without type-B QPO, where the ratios (type-B QPO/broadband noise) show a maximum at around 4 keV and then decrease gradually towards high energies. Finally, we discuss the possible change of the geometry of the inner accretion flow and/or jet during the transitions.

Key words: accretion, accretion discs - black hole physics - X-rays: binaries

1 INTRODUCTION

Low-mass black hole X-ray binaries (BHXBs) consist of a stellarmass black hole accreting matter from its companion star. These systems spend most of the time in a quiescent state, and occasionally go into bright outbursts due to the hydrogen-ionization instability in the outer part of the accretion disc (Lasota 2001). Black hole transients in outburst usually evolve through different spectral states with changing luminosity (see McClintock & Remillard 2006, for a review). At the beginning of the outburst, a source is usually detected in a hard state (HS), where the energy spectrum is dominated by a Comptonization component with a power-law photon index of ~1.4– 1.7 (Méndez & van der Klis 1997; Zdziarski & Gierliński 2004). As the accretion rate increases, the thermal component gradually strengthens and the source evolves into the intermediate state (IMS). We can further divide the IMS into a hard-intermediate state (HIMS) and a soft-intermediate state (SIMS), according to the spectral and timing properties (Homan & Belloni 2005). When the thermal component dominates the spectrum, the source enters into a soft state (SS), where the inner radius of the disc is thought to reach the innermost stable circular orbit (ISCO, e.g., Done et al. 2007). At the end of the outburst, the source fades quickly and moves back to the HS via the IMS in reverse order (Belloni & Motta 2016).

For BHXBs, not only the spectral shape but also the timing properties change significantly during an outburst. Fourier analysis provides a simple and intuitive way to inspect the fast timing variability. Narrow and strong peaks with frequencies ranging from a few mHz to \sim 30 Hz, called low-frequency quasi-periodic oscillations (LFQ-POs), are usually detected in the power density spectra (PDS) of these sources. Based on the properties of the PDS, LFQPOs can be

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divided into three types, i.e., type-A, B and C (Casella et al. 2005). Among the three types of QPOs, type-C QPOs are the most common type mostly appearing in the HS and HIMS. These OPOs are usually accompanied by strong flat-top noise variability. Although the physical origin of the type-C QPOs is still under debate, some evidence shows that they likely originate from the Lense-thirring precession of the inner hot flow or jet (Ingram et al. 2009; Ingram & Done 2010, 2011; Kalamkar et al. 2016; Huang et al. 2018; Bu et al. 2021; Ma et al. 2021; Méndez et al. 2022). However, this model faces considerable challenges both theoretically and observationally (Marcel & Neilsen 2021; Nathan et al. 2022). Zhang et al. (2022a) fitted the time-dependent Comptonization model to the type-C QPOs in MAXI J1535-571. Type-B QPOs have been detected in a number of sources; the appearance of these QPOs defines the start of the SIMS (Belloni & Motta 2016). The type-B QPOs were found to occur close in time to the launch of discrete jet ejecta (Fender et al. 2004, 2009; Homan et al. 2020; Carotenuto et al. 2021). Using phase-resolved spectroscopy, Stevens & Uttley (2016) found that the spectral parameters change as a function of QPO phase, leading to a geometric interpretation for type-B QPOs. Kylafis et al. (2020) proposed a precessing jet model, which could reproduce the periodic variation of Γ with QPO phase. García et al. (2021a) and Peirano et al. (2023), on the other hand, fitted the rms and lag spectra of the type-B QPO in MAXI J1348-630 and GX 339-4, respectively, with a time-dependent Comptonization model (Karpouzas et al. 2020; Bellavita et al. 2022), in which the QPO properties are due to coupled oscillations of the corona and the disc. Type-A QPOs are the least common type of QPOs and have been rarely studied (Ingram & Motta 2019). No comprehensive model has been proposed to explain type-A QPOs.

Rapid transitions between different types of PDS happening over several tens of seconds have been observed in several BHXBs. Such transitions are usually observed in the IMS and always involve type-B QPOs. The study of these transitions can provide important evidence on what triggers the OPO phenomenon and on the physical origin of QPOs in general. Type-C QPO switching to/from type-B QPO is usually detected during the HIMS-SIMS state transitions, along with significant spectral variations (e.g., Soleri et al. 2008; Motta et al. 2011; Homan et al. 2020). Type-B/A QPO transitions have been found in GX 339-4 (Miyamoto et al. 1991; Nespoli et al. 2003; Motta et al. 2011), XTE J1550-564 (Homan et al. 2001; Sriram et al. 2016), XTE J1859+226 (Casella et al. 2004; Sriram et al. 2013), XTE J1817-330 (Sriram et al. 2012) and H 1743-322 (Homan et al. 2005). In addition, LFQPOs are typically transient that can appear/disappear on short timescales of several seconds. Recently, Xu et al. (2019) reported a sudden turn-on of a transient type-C QPO accompanied by a rapid decrease in X-ray flux in Swift J1658.2-424. Zhang et al. (2021) made a systematic analysis of the transient type-B QPO detected in MAXI J1348-630 using observations with the Neutron Star Interior Composition Explorer (NICER). They found that the transient nature of the QPO is associated with a redistribution of the accretion power between the disc and the Comptonizing region. Meanwhile, Liu et al. (2022b) fitted the broadband Insight-HXMT spectra of periods with and without the type-B QPOs, and found a slight decrease in the height of the corona when the QPO disappears.

GX 339–4 is a BHXB with a mass function of $1.91 \pm 0.08 \text{ M}_{\odot}$ (Heida et al. 2017). It experienced frequent outbursts in the past two decades with a ~2-yr cycle, making it one of the most studied stellar-mass black holes (Makishima et al. 1986; Zdziarski et al. 2004). GX 339–4 entered a new outburst in 2021 (Tremou et al. 2021; Pal et al. 2021; Garcia et al. 2021b; Sguera et al. 2021), showing all four typical spectral states found in BHXBs. Both *NICER* and *Insight*-

Table 1. Log of the *NICER* and *Insight*-HXMT observations used in this paper.

No.	ObsID	Start time	Exposure (s)				
NICER							
#1	4133010105	2021 March 28 00:28:40	13605				
#2	4133010106	2021 March 29 02:38:28	10702				
#3	4133010107	2021 March 30 00:19:57	13793				
#4	4133010108	2021 March 31 01:07:00	10184				
Insight-HXMT							
#1	P030402403913	2021 March 29 12:22:02	1890				
#2	P030402403914	2021 March 29 15:32:44	2490				
#3	P030402403920	2021 March 30 13:13:50	2040				
#4	P030402403921	2021 March 30 16:24:34	2580				
#5	P030402403922	2021 March 30 19:35:18	2910				
#6	P030402403923	2021 March 30 22:46:03	2520				
#7	P030402403924	2021 March 31 01:56:47	2250				
#8	P030402403925	2021 March 31 05:07:31	1140				
#9	P030402403926	2021 March 31 08:18:16	1530				
#10	P030402403927	2021 March 31 11:29:00	1740				
#11	P030402403928	2021 March 31 14:39:45	2160				
#12	P030402403929	2021 March 31 17:50:29	2760				
#13	P030402403930	2021 March 31 21:01:13	2820				

HXMT performed high-cadence observations of this outburst. Using quasi-simultaneous data of *NICER* and *Insight*-HXMT, in this paper we report the study of the fast transitions between different types of PDS observed in the IMS of this source. The large effective areas and broad energy coverage of these observations with *NICER* and *Insight*-HXMT enable us to investigate in detail the changes of the spectral-timing properties during the fast transitions. Especially, we can constrain the disc, Comptonization and reflection components simultaneously by jointly fitting the *NICER* and *Insight*-HXMT spectra. We also compare the fast transitions in GX 339–4 with those observed in the newly discovered BHXBs MAXI J1820+070 and MAXI J1348–630. In Section 2, we describe the observation and data reduction. The data analysis and main results are presented in Section 3. We discuss our main results in Section 4, and summarize our conclusions in Section 5.

2 OBSERVATIONS AND DATA REDUCTION

The MAXI/GSC light curve and the evolution of the hardness ratio are shown in Fig.1. The hardness ratio evolves from a high value of \sim 1 to a low value of \sim 0.2 and back to a high value at the end of the outburst. This suggests that the source experienced a full outburst with an initial hard-to-soft transition and a soft-to-hard transition. We refer to Peirano et al. (2023) for the detailed evolution track observed with NICER. NICER observed that the flux of GX 339-4 exhibited a dramatic increase from ~ 2500 counts s⁻¹ on 2021 Mar 26 (MJD 59299) to ~4600 counts $\rm s^{-1}$ on 2021 Mar 28 (MJD 59301; Wang et al. 2021). Multi-wavelength observations indicated that GX 339-4 was already in the HIMS, and was evolving rapidly towards the SIMS (Wang et al. 2021; Baglio 2021; Corbel et al. 2021; Liu et al. 2021). Both NICER and Insight-HXMT conducted very intense observation campaigns during this epoch that covered a complete state transitions between the HIMS and the SIMS. During the state transition, we observed fast alternations between different types of PDS. In this paper, we focus on the observations during



Figure 1. The evolution of 2–20 keV count rates and hardness ratio (4–10 keV/2–4 keV) of GX 339–4 in its 2021 outburst captured by MAXI/GSC. The red region marks the time interval we studied in this paper.

Table 2. Best-fitting spectral parameters for the spectra of GX 339–4 in the period with broadband noise (BLN), type-B QPO (BQ), and without any QPO (NQ), fitted with model 1: CONSTANT*TBABS*(DISKBB+NTHCOMP+NTHRATIO*RELXILLCP). The spectra are combined from multiple consecutive orbits showing a similar PDS shape to improve the signal-to-noise ratio. The time intervals used to create the spectra are shown in Fig. 2 with different colors (blue for BLN, gray for BQ and magenta for NQ).

Component	Parameters	BLN	BQ	NQ
Constant		0.89 ± 0.01	0.85 ± 0.01	0.85 ± 0.01
Tbabs	$N_{\rm H}(\times 10^{22}{\rm cm}^{-2})$		0.46 ± 0.01	
Diskbb	kT _{in} (keV) norm	$\begin{array}{c} 0.71 \pm 0.01 \\ 2551 \substack{+108 \\ -53} \end{array}$	$\begin{array}{c} 0.77 \pm 0.01 \\ 2342^{+82}_{-62} \end{array}$	$\begin{array}{c} 0.78 \pm 0.01 \\ 2556^{+63}_{-51} \end{array}$
Nthcomp		2.16 ± 0.01	2.21 ± 0.01	2.20 ± 0.01
	kI _e (keV) norm	$0.29^{+0.04}_{-0.02}$	100 (fix) 0.19 ± 0.06	0.13 ± 0.04
RelxillCp	$i (°)$ a $R_{in}(ISCO)$ $R_{out}(R_g)$ z Index $\log (\xi)$ $\log N (cm^{-3})$	-1.55 ± 0.06 3.50 ± 0.09 2.99 ± 0.03 $20.00^{+}P_{0.05}^{+}$	34.14 ± 1.00 0.998 (fix) -1.63 \pm 0.06 400 (fix) 0 (fix) 3.58 \pm 0.10 2.99 \pm 0.04 20.00 ⁺ P ⁴ _{0.05}	$-1.71^{+0.13}_{-0.08}$ 3.45 ± 0.09 3.00 ± 0.06 $19.73^{+0.12}_{-0.22}$
	$A_{\rm Fe}$ $kT_{\rm e}$ (keV) norm	-0.05 0.013 ± 0.001	$\begin{array}{r} -0.08\\ -0.08\\ 3.34_{-0.50}^{+0.87}\\ 100 \text{ (fix)}\\ 0.012 \pm 0.001\end{array}$	-0.22 0.010 ± 0.001
Flux				
Fdiskbb	$(10^{-8} \text{ erg cm}^{-2} \text{ s}^{-1})$	0.87 ± 0.01	1.17 ± 0.01	1.31 ± 0.01
F _{nthcomp}	$(10^{-8} \text{ erg cm}^{-2} \text{ s}^{-1})$	0.24 ± 0.01	0.16 ± 0.01	0.11 ± 0.01
FrelxillCp	$(10^\circ \text{ erg cm}^2 \text{ s}^2)$	0.53 ± 0.01	0.49 ± 0.01	0.39 ± 0.01
R _f		2.21 ± 0.10	3.06 ± 0.20	3.54 ± 0.33
	$\chi^2/d.o.f$.		1026/1202	

[†]: The letter (P) indicates that the error of the parameter pegged at the upper boundary.

this transition period; the logs of the observations for *NICER* and *Insight*-HXMT we used in this paper are listed in Table 1.

NICER is a soft X-ray telescope onboard the International Space Station (ISS), launched on 2017 June 3. It provides high throughput in the 0.2–12 keV energy band with an absolute timing precision of

~100 ns, making it an ideal instrument to study fast X-ray variability. *NICER* consists of 56 co-aligned concentrator X-ray optics, each paired with a single-pixel silicon drift detector. Presently, 52 detectors are active with a peak effective area of ~1900 cm⁻² at 1.5 keV. In our analysis, we exclude data from detectors #14 and #34 as



Figure 2. Evolution of the *NICER* 0.5-10 keV light curve, hardness ratio (6.0–10.0 keV/2.0–4.0 keV), together with the *Insight*-HXMT LE (1.0–10 keV), ME (8.0–35.0 keV), and HE (35.0–200.0 keV) light curves of GX 339–4 for the period we study. The different shaded regions mark the time intervals we used to create the PDS and energy spectra for different types of variability (see the text for details).



Index of PDS

Figure 3. *NICER* 0.5–10 keV light curve with 16-s binning (upper panel) and corresponding dynamical power density spectrum (lower panel) of GX 339–4 for the period we study. All time gaps are removed and marked with dotted lines in the upper panel. Four different types of variability are identified based on the light curve and timing properties. The blue, gray and green shaded regions mark the periods with a relatively strong broadband noise component, a type-B QPO, and the flip-flop phenomenon in the PDS, respectively. The magenta shaded region represents the periods when the PDS are dominated by Poisson noise (see the text for details).



Figure 4. Representative power density spectra of GX 339–4 using the *NICER* 0.5–10 keV band. *Panel a*: PDS with a strong band-limited noise component, extracted from the time interval MJD 59302.50–59302.77. *Panel b*: PDS with a typical type-B QPO, extracted from the time interval MJD 59303.60–59304.12. *Panel c*: PDS dominated by Poisson noise without any peaks, extracted from the time interval MJD 59304.18–59304.97.

they occasionally show episodes of increased instrumental noise. We processed the *NICER* observations using the *NICER* software tools NICERDAS version 8.0 in HEASOFT version 6.29. We run the pipeline nicerl2 with the standard filtering criteria.

Insight-HXMT is China's first X-ray astronomy satellite, launched on 2017 June 15 (Zhang et al. 2020a). It carries three slatcollimated instruments: the High Energy X-ray telescope (HE, poshwich NaI/CsI, 20–250 keV, Liu et al. 2020), the Medium Energy X-ray telescope (ME, Si pin detector, 5–30 keV, Cao et al. 2020), and the Low Energy X-ray telescope (LE, SCD detector, 1–15 keV, Chen et al. 2020). The *Insight*-HXMT observations are extracted from all three instruments using the *Insight*-HXMT Data Analysis software (HXMTDAS) v2.05¹, and filtered with the following criteria: (1) pointing offset angle less than 0.04° ; (2) Earth elevation angle larger than 10° ; (3) geomagnetic cutoff rigidity larger than 8 GeV; (4) at least 300 s before and after the South Atlantic Anomaly passage. Each instrument of *Insight*-HXMT carries large, small and blind field-of-

¹ The data analysis software is available from http://hxmten.ihep.ac. cn/software.jhtml.



Figure 5. Left panel: a representative light curve of the flip-flop variability in GX 339–4 with 1-s binning. The data are extracted from the time interval MJD 59302.37–59302.44. We divided the light curve into a high-flux and a low-flux interval based on the blue dashed line. The time origin is MJD 59302.3710. Middle and right panels: the average power spectra for the high-flux (red) and low-flux interval (black) of the flip-flop period in GX 339–4. The data used to produce the power spectra are shown in Fig. 2 with green.

Table 3. Best-fitting spectral parameters for the spectra of GX 339–4 in the period with broadband noise (BLN), type-B QPO (BQ), and without any QPO (NQ), fitted with model 2: CONSTANT*TBABS*(DISKBB+NTHCOMP+NTHRATIO*RELXILLEPCP). The spectra are combined from multiple consecutive orbits showing a similar PDS shape to improve the signal-to-noise ratio. The time intervals used to create the spectra are shown in Fig. 2 with different colors (blue for BLN, gray for BQ and magenta for NQ).

Component	Parameters	BLN	BQ	NQ
Constant		0.89 ± 0.01	0.85 ± 0.01	0.85 ± 0.01
Tbabs	$N_{\rm H}(\times 10^{22} {\rm cm}^{-2})$		0.46 ± 0.01	
Diskbb	<i>kT</i> _{in} (keV) norm	$\begin{array}{c} 0.71 \pm 0.01 \\ 2592^{+71}_{-52} \end{array}$	$\begin{array}{c} 0.77 \pm 0.01 \\ 2351^{+43}_{-34} \end{array}$	$\begin{array}{c} 0.78 \pm 0.01 \\ 2586^{+37}_{-30} \end{array}$
Nthcomp	Γ	2.14 ± 0.02	2.19 ± 0.01	2.18 ± 0.02
	kT _e (keV) norm	0.27 ± 0.04	100 (fix) 0.18 ± 0.03	0.12 ± 0.03
RelxilllpCp	<i>i</i> (°) <i>a</i>		29.90 ^{+0.94} -1.38 0.998 (fix)	
	$R_{\rm in}(\rm ISCO)$ $R_{\rm orb}(R_{\rm orb})$	-1.71 ± 0.03	-1.84 ± 0.04	-1.87 ± 0.07
	$h(R_g)$	$1.49^{+0.32}_{-0.21}$	$1.49^{+0.11}_{-0.20}$ 0 (fix)	$1.96^{+0.32}_{-0.38}$
	$\log(\xi)$	2.99 ± 0.04	$2.98 \pm +0.03$	$3.01^{+0.06}_{-0.04}$
	$\log N \ (\mathrm{cm}^{-3})$ A_{Fe}	$20.00^{+P^{\dagger}}_{-0.08}$	$20.00^{+P^{\dagger}}_{-0.08}$ $3.51^{+0.59}_{-0.41}$ $100(6x)$	$19.94_{-0.26}^{+P^{\dagger}}$
	norm	$2.91_{-1.79}^{+0.77}$	$2.66^{+1.56}_{-1.24}$	$0.30^{+0.63}_{-0.13}$
Flux				
F _{diskbb}	$(10^{-8} \text{ erg cm}^{-2} \text{ s}^{-1})$	0.89 ± 0.01	1.20 ± 0.01	1.31 ± 0.01
Fnthcomp	$(10^{-8} \text{ erg cm}^{-2} \text{ s}^{-1})$	0.23 ± 0.01	0.16 ± 0.01	0.10 ± 0.01
FrelxillpCp	$(10^{-8} \text{ erg cm}^{-2} \text{ s}^{-1})$	0.54 ± 0.01	0.50 ± 0.01	0.40 ± 0.01
R _f		2.34 ± 0.11	3.12 ± 0.20	4.00 ± 0.41
	$\chi^2/d.o.f$.		993/1202	

[†]: The letter (P) indicates that the error of the parameter pegged at the upper boundary.



Figure 6. Best-fitting spectral model and residuals for the spectra of GX 339–4 in the period with broadband noise (blue), type-B QPO (gray) and without any QPO (magenta), fitted with model 1: CONSTANT*TBABS*(DISKBB+NTHCOMP+NTHRATIO*RELXILLCP).

view (FoV) detectors in order to facilitate background analysis. The small FoV detectors (LE: $1^{\circ}.6 \times 6^{\circ}$; ME: $1^{\circ} \times 4^{\circ}$; HE: $1^{\circ}.1 \times 5^{\circ}.7$) have a lower probability of source contamination. Therefore, to avoid possible contamination from the bright Earth and nearby sources, we only use data from the small FoV detectors (Chen et al. 2018).

3 ANALYSIS AND RESULTS

3.1 Fast transitions between different types of PDS

In Fig. 2 we plot the evolution of the *NICER* 0.5–10 keV count rate, hardness ratio (6.0–10.0 keV/2.0–4.0 keV), along with the *Insight*-HXMT/LE 1.0–10.0 keV, ME 8.0–35.0 keV, and HE 35.0–200.0 keV light curves of the period we study. The data of *Insight*-HXMT/HE are dominated by background, so that we did not use them for our further analysis. From this figure, it is apparent that the source exhibited dramatic flux changes, mainly jumping between a low- and

a high-flux state, accompanied by significant changes in spectral hardness.

For our timing analysis, we create dynamical and average PDS in the *NICER* 0.5–10.0 keV energy band with 16-s data segments and 1/256-s time resolution. We normalised the PDS to rms²/Hz (Belloni & Hasinger 1990; Miyamoto et al. 1991), and subtracted the contribution due to Poisson noise. In this work we only show the timing results of the *NICER* data, since the *NICER* count rate is an order of magnitude higher than that of *Insight*-HXMT and, therefore, the features, i.e., broadband noise or QPOs, are more significant in the PDS of *NICER*.

In Fig. 3, we show the *NICER* 0.5–10 keV light curve with 16-s binning and the corresponding dynamical PDS of the same period as in Fig. 2. All time gaps are removed in this plot and marked with dotted lines. The *x*-axis represents the index of each 16-s PDS. The same plot of each individual observation is shown in Fig. A1. From the dynamical PDS, it is apparent that the shape of the PDS varies significantly between different orbits, coinciding with changes in flux



Figure 7. Best-fitting spectral model and residuals for the spectra of GX 339–4 in the period with broadband noise (blue), type-B QPO (gray) and without any QPO (magenta), fitted with model 2: CONSTANT*TBABS*(DISKBB+NTHCOMP+NTHRATIO*RELXILLEPCP).

and spectral hardness (see also Fig. 2). Based on their different timing characteristics, we can divide the PDS of this period into three types. In Fig. 4, we show the representative PDS of each type. In the upper panel of Fig. 3, we have marked the time of the PDS shown in Panels (a), (b) and (c) with blue, gray and magenta, respectively.

The PDS as the one shown in Panel (a) of Fig. 4 usually appear at a low-flux state when the count rate is below \sim 5200 count s⁻¹, corresponding to a higher hardness ratio. These PDS are dominated by a relatively strong broadband noise component with a 0.1–128 Hz fractional rms amplitude above 5% (hereafter we call 'BLN' to this type of PDS). Sometimes weak type-C QPOs (not always visible) are detected at around 5–7 Hz. This type of PDS is consistent with that typically observed at the end of the HIMS (Stiele et al. 2011; Homan et al. 2020). The PDS as the one shown in Panel (b) are detected at a high-flux state, corresponding to a slightly softer spectral hardness. Their overall rms amplitude value, ~2% in the 0.1–128 Hz, is significantly lower than that of the PDS shown in Panel (a). A sharp narrow 5-Hz QPO (quality factor² $Q \sim 7$) is seen with a fractional rms amplitude of ~1.7%. The centroid frequency of the QPO remains more or less constant with time. Based on these characteristics, we can identify this as a type-B QPO (hereafter we call 'BQ' to this type of PDS). The type-B QPOs are usually observed when a source enters the SIMS (Belloni & Motta 2016). Still at a high-flux level, when the type-B QPO disappears, we observe the PDS as the one shown in Panel (c). In this case, the energy spectrum is softer than in the periods shown in Panels (a) and (b). The PDS is dominated by Poisson noise without any significant peak. The 0.1–128 Hz fractional rms is below 1%. This is the typical PDS observed in the SS of BHXBs (hereafter we call 'NQ' to this type of PDS).

It is important to mention that we also observed a peculiar kind of light curve in some orbits of this period (green in Fig. 3): the

 2 $Q = v_{0}$ /FWHM, where v_{0} is the centroid frequency of the QPO and FWHM is the full width at half maximum.

source undergoes rapid transitions between a low- and a high-flux state on timescales of several tens of seconds. In the left panel of Fig. 5, we show a representative light curve of this type. This type of variability, called flip-flops, has been observed in previous outbursts of GX 339–4 (Miyamoto et al. 1991) and in some other sources, e.g., Swift J1658.2-4242 (Bogensberger et al. 2020), GS 1124-683 (Takizawa et al. 1997) and XTE J1550-564 (Homan et al. 2001; Sriram et al. 2016). We then split the light curve into a high-flux (above the blue dashed line) and a low-flux interval (below the blue dashed line). The PDS of the two intervals are shown in the middle and right panels of Fig. 5. We find that the PDS of the high-flux interval is similar to that shown in Panel (b) of Fig. 4. A significant 5-Hz QPO is seen with weak broadband noise. The PDS of the low-flux interval is dominated by a low-frequency noise component.

3.2 Energy spectra corresponding to different types of PDS

We extract representative energy spectra corresponding to the different types of PDS shown in Fig. 4. For our spectral analysis, we use NICER for the low-energy spectral coverage and Insight-HXMT/ME for the high-energy spectral coverage. We do not use the Insight-HXMT/HE data due to the high background contribution. We create the NICER background-subtracted spectra with the Background Estimator Tool 'nibackgen3C50'³. We binned the spectra in accordance with the optimal binning algorithm proposed by Kaastra & Bleeker (2016) with a minimum of 50 counts per spectral bin. We then added a systematic error of 1% percent below 3.0 keV using GRPPHA. We produced the Insight-HXMT/ME spectra using the HXMT pipeline. The energy bands adopted for spectral analysis are 1.0-10.0 keV for NICER (we ignore the data below 1.0 keV due to the considerable instrumental residuals) and 10-25 keV for Insight-HXMT/ME. We fit the three representative spectra jointly using XSPEC version 12.12.10 (Arnaud 1996).

For our spectral fitting, we first use a simple continuum model consisting of an absorbed disc component and a Comptonization component, CONSTANT*TBABS*(DISKBB+NTHCOMP) in XSPEC. The CON-STANT reflects the relative calibration between NICER and Insight-HXMT/ME, and is fixed to 1 for NICER and left free to vary for Insight-HXMT/ME. We find a strong and broad Fe K emission line centered at 6-7 keV in the residuals, accompanied by a weak reflection hump above 10 keV. We, therefore, include a full reflection model in our fitting (García et al. 2014; Dauser et al. 2014, 2016, 2022). We have tried the relativistic reflection models within an empirical broken power-law emissivity (RELXILLCP) and that with the emissivity inferred from the lamp-post geometry (RELXILLIPCP). It is worth noting that both RELXILLCP and RELXILLIPCP calculate the relativistic disc reflection spectra using seed photon spectra of NTHCOMP fixed at 0.01 keV. This is compatible with a cutoff powerlaw, and very different from the typical illuminating spectra (DISKBB temperature ~ 0.5 keV) observed in BHXBs, thus introducing an artificial soft-excess in the modeling. To improve this issue, we use the multiplicative model NTHRATIO⁴, which aims to correct for this soft excess by introducing a first-order phenomenological correction, renormalising the reflected spectrum by the ratio between the NTHCOMP models at kT_{bb} and the fixed value of 0.01 keV. The model depends on three parameters, i.e., Γ , kT_e and kT_{bb} , which we link to Γ , kT_e , kT_{bb} from the fitted NTHCOMP and DISKBB components. This effectively does not add extra parameters to the model. Therefore, our final models to describe the spectra are model 1: CONSTANT*TBABS*(DISKBB+NTHCOMP+NTHRATIO*RELXILLCP), and model 2: CONSTANT*TBABS*(DISKBB+NTHCOMP+NTHRATIO* RELX-ILLLPCP).

In both models, we linked the hydrogen column density $(N_{\rm H})$, inclination and the iron abundance together between the spectra of the three epochs as they are not likely to change in such a short period. Since GX 339-4 is found to harbor a near maximally spinning black hole (Ludlam et al. 2015; Parker et al. 2016), we fix the value of the spin at $a_* = 0.998$ to check the possible change of the inner disk radius. Since the high-energy cutoff of the hard component is outside the energy range of the instrument, we fix the electron temperature $(kT_{\rm e})$ at 100 keV. We separate the disc reflection component and the illuminating Comptonization component by fixing the reflection fraction (R_f) at -1 and we calculate R_f from the flux of the reflection and the Comptonization component we measured. In model 1, we assume a single power-law emissivity profile. Using a broken powerlaw emissivity profile results in overfitting of the spectra. In model 2, the effect of returning radiation on the shape of the X-ray reflection spectrum is considered (Dauser et al. 2022). The other parameters in both models are allowed to vary between spectra. Both models give an acceptable spectral fit with $\chi^2/d.o.f. = 1026/1202$ for model 1 and $\chi^2/d.o.f. = 993/1202$ for model 2. The best-fitting spectral models and residuals are shown in Fig. 6 and Fig. 7, and the bestfitting spectral parameters are listed in Table 2 and Table 3.

From Tables 2 and 3, it is apparent that the evolution of the main spectral parameters is very similar between the two models. The inner disc radius, R_{in} , measured from the reflection spectrum is consistent within errors between the spectra of the three epochs. However, the normalisation of the disc component varies moderately. The change of the DISKBB normalisation could be due to the change of the spectral hardening factor. By fitting the Insight-HXMT broadband spectra of the 2021 outburst of GX 339-4, Liu et al. (2022a) found that the inner disc radius remains stable during the HIMS-SIMS state transition. If $R_{\rm in}$ does not change, the change of the DISKBB normalisation could be due to the change of the spectral hardening factor (Kubota et al. 1998). In this case, we find that the spectral hardening factor in the BLN, BQ and NQ epochs is 1.25 ± 0.02 , 1.32 ± 0.02 , $1.32^{+0.03}_{-0.05}$ for model 1, and 1.32 ± 0.01 , 1.40 ± 0.02 , 1.38 ± 0.03 for model 2 by assuming $i = 30^\circ$, D = 8 kpc, $M_{\rm BH} = 10 M_{\odot}$. Therefore, minor changes in the spectral hardening factor could account for the changes of the DISKBB normalisation. The change of the spectral hardening factor could be due to the change of the disc density (Zhang et al. 2022b) or the illumination of the hard X-rays from the corona onto the disc (Ren et al. 2022).

From BLN to BQ, the inner disc temperature increases with a slight spectral softening. The reflection fraction increases gradually from BLN to BQ to NQ. The height of the corona measured from model 2 does not change too much between the spectra of the three epochs. However, we note that their values ($h \sim 1.5 - 2.0R_g$) are very small, which would indicate that the illuminating source is very close to the black hole.

3.3 Comparison with MAXI J1820+070 and MAXI J1348-630

In this section, we compare the transitions we observed in GX 339–4 with those seen in the two bright BHXBs MAXI J1820+070 and MAXI J1348–630.

A rapid HIMS-to-SIMS state transition was observed in MAXI J1820+070 by *NICER* (ObsID: 1200120197), along with fast changes

³ https://heasarc.gsfc.nasa.gov/docs/nicer/tools/nicer_ bkg_est_tools.html

⁴ https://github.com/garciafederico/nthratio



Figure 8. For GX 339–4, MAXI J1820+070 and MAXI J1348–630, upper panel: ratio between the spectrum with and without the type-B QPO (BQ/NQ), and lower panel: ratio between the spectrum with the type-B QPO and that with the broadband noise (BQ/BLN). The green points mark the spectral ratio between the high-flux level and the low-flux level of the flip-flop variability. The data of MAXI J1348–630 are adopted from Liu et al. (2022b). The data points are re-binned for clarity.

in the X-ray variability (Homan et al. 2020). A type-C QPO seen at the beginning of the transition became gradually weaker and was replaced by a type-B QPO at some point. About 2–2.5 hours after this switch, a strong radio flare was observed that corresponded to the launch of jet ejecta (Homan et al. 2020). The type-B QPO was only present for ~1.5 hours and then disappeared. For our analysis, we processed this observation with the standard filtering criteria using NICERDAS version 8.0. We then extracted backgroundsubtracted spectra for the period with type-C QPO (BLN), type-B



Figure 9. The change of the Comptonization component flux as a function of the change of the disk component flux from non-QPO to type-B QPO for GX 339–4, MAXI J1820+070 and MAXI J1348–630. The fluxes are calculated in the 0.6–10.0 keV and are in units of 10^{-8} erg cm⁻² s⁻¹. The dashed line represents the best-fitting line $\Delta F_{\text{nthcomp}} = -1.03\Delta F_{\text{diskbb}} - 0.09$.



Figure 10. Flux fraction of the DISKBB component (F_{disk}/F_{total} , upper panel) and the NTHCOMP component ($F_{nthcomp}/F_{total}$, lower panel) as a function of the total flux of GX 339–4 for each orbit with (black) or without (red) the type-B QPO.

QPO (BQ), and without any QPOs (NQ), respectively. We fitted the *NICER* spectra with the model TBABS*(DISKBB+NTHCOMP+GAUSS) in the 1.5–10.0 keV band. The data below 1.5 keV are not used due to the large instrumental residuals seen in the spectra. Unfortunately, *Insight*-HXMT did not conduct observations during this transition.

For MAXI J1348–630, fast transitions between different kinds of PDS were detected by *NICER* (Zhang et al. 2021) and *Insight*-HXMT (Liu et al. 2022b). Using *Insight*-HXMT data, Liu et al. (2022b) detected multiple cases of BQ-NQ and BLN-BQ transitions in this source and presented a detailed spectral analysis in a broad energy band of 1–100 keV. Zhang et al. (2021) reported the detection of a fast appearance/disappearance of a type-B QPO (BQ-NQ transition) in four *NICER* observations and performed the first systematic spectral-timing analysis of this transition. The results of MAXI J1348–630 shown in this paper are adopted from Liu et al. (2022b) and Zhang et al. (2021).

In the upper panel of Fig. 8, we show the ratio between the spectra with and without the type-B QPO (BQ/NQ). The data of MAXI J1348–630 are adopted from the upper panel of fig.6 of Liu et al. (2022b). The overall trend of the spectral ratio is quite similar between the three black hole systems. The main spectral differences appear at energies above 3 keV, where the ratio increases towards higher energies and turns to flat or slightly decreases with energy above 10 keV. The values of the ratio above 10 keV are different between sources and between different cases of the same source. The spectral ratios below 3 keV are all lower than unity, suggesting a weaker disc component when there is a type-B QPO than when there is no QPO.

The upper panel of Fig. 8 shows that the high-energy emission is stronger when the type-B QPO appears. Then it is natural to consider that the type-B QPO is related to the appearance of an additional hard spectral component. To test this scenario, we perform a joint spectral fitting for the BQ and NO spectra using a two-Comptonized component model, con-STANT*TBABS*(DISKBB+NTHCOMP1+NTHCOMP2+LAOR) in XSPEC. In our fitting, the parameters of the first Comptonization component (NTHCOMP1) including Γ , kT_e , kT_{bb} , norm are linked between the BQ and NQ spectra. We assume that the type-B QPO is only produced in the second Comtonization component (NTHCOMP2) and the normalization of this component is set to zero for the NO spectrum. We obtain that the NTHCOMP2 component contributes ~22% of the flux to the BQ spectrum. If NTHCOMP1 does not contribute to the QPO rms amplitude, we measure that the intrinsic rms amplitude of NTHCOMP2 should be around 71% to produce the observed QPO rms (16% in the 20-30 keV band). We have also done a similar analysis for MAXI J1348-630 and the intrinsic rms of the additional hard component should be higher than 100% to produce the 15% rms of the type-B QPO. However, the rms of the variability in BHXBs is typically lower than 50% (Ingram & Motta 2019). Therefore, it is not likely that only the increased hard component flux contributes to the OPO rms.

Based on a systematic analysis of the transient type-B QPO in MAXI J1348–630, Zhang et al. (2021) found that, in the *NICER* energy band (0.6–10 keV), the change of the Comptonization component flux, $\Delta F_{\text{nthcomp}}$, is anti-correlated with the change of the disc component flux, ΔF_{diskbb} , during the BQ-NQ transition (see their fig. 8). This suggests that the appearance of the type-B QPO is related to a redistribution of the accretion power between the disc and the Comptonization component. In Fig. 9, it is apparent that the three sources, GX 339–4, MAXI J1820+070 and MAXI J1348–630, follow the same correlation. We fit this correlation using a linear function and find the best-fitting line is $\Delta F_{\text{nthcomp}} = -1.03\Delta F_{\text{diskbb}} - 0.09$,

consistent with the result of Zhang et al. (2021) obtained using the data of MAXI J1348–630 only.

By comparing the spectra of the orbits with and without type-B QPO, Zhang et al. (2021) found a clear threshold in the fraction of the Comptonization component flux to the total flux ($F_{nthcomp}/F_{total}$, 0.6–10 keV band), which is related to the appearance of type-B QPO: the QPO only appears when $F_{nthcomp}/F_{total} \gtrsim 40\%$. Following the method described in Zhang et al. (2021), we make a similar analysis for GX 339–4 using *NICER* data. In Fig. 10 we show F_{disk}/F_{total} (top panel) and $F_{nthcomp}/F_{total}$ (bottom panel) against the total flux. Here each point corresponds to one orbit from the BQ/NQ epoch in Fig. 3. We also find a clear threshold in $F_{nthcomp}/F_{total}$ or F_{diskbb}/F_{total} in this plot. The QPO is present when $F_{nthcomp}/F_{total} \gtrsim 70\%$.

In the lower panel of Fig. 8, we show the ratio between the spectra with type-B QPO and those with the broadband noise (BQ/BLN). The data of MAXI J1348-630 are adopted from the lower panel of fig.6 of Liu et al. (2022b). The spectral ratios of BQ/BLN are quite different from those of BQ/NQ. Below ~10 keV, the ratios are greater than unity, and first increase and then decrease with energy, showing a maximum at around 4 keV. Above ~10 keV, the ratios are lower than unity and decrease towards higher energies up to 100 keV with a different slope. We also extract a spectrum for the high-flux level and the low-flux level of the flip-flop variability, respectively. The spectral ratio (high-flux/low-flux) is shown in the lower panel of Fig. 8 with green points. We find that below ~4 keV, the spectral ratio increases monotonously with energy, similar to that of BQ/BLN. However, above ~ 4 keV, the evolution of the spectral ratio is quite different. The spectral ratio between the high-flux and low-flux level of the flip-flops remains more or less constant without showing a decreasing trend. In addition, we note that no anti-correlation between the change of the thermal and Comptonization component flux is seen during the BLN/BQ transition. This can be inferred from the evolution of the spectral ratio with energy easily as the spectral ratio is always greater than unity below 10 keV.

4 DISCUSSION

Fast transitions in X-ray variability have been reported in several sources during the past three decades. Thanks to the large effective area of NICER and Insight-HXMT, we can study, for the first time, in detail the spectral and variability changes during the fast transitions in a broad energy band. In this paper, we have investigated the changes of the spectral-timing properties during the fast transitions observed in GX 339-4, and made a detailed comparison of the transitions between different black hole systems. We find that the spectral ratio between intervals with a type-B QPO (BQ) and without a QPO (NQ) is nearly constant or slightly decreasing above 10 keV, and the value of the constant is different between sources. Below 10 keV, a change in the relative contribution of the disc and Comptonization emission was observed during the BQ and NQ transitions. The type-B QPOs were only detected when the fraction of the Comptonization component is above a threshold. The value of the threshold is found to be different between sources. In addition, the trend of the spectral ratio is quite different between the two different kinds of transition (BQ/NQ and BQ/BLN). Below we discuss our main findings.

4.1 The transient nature and physical origin of the type-B QPO

Type-B QPOs are typically transient features that suddenly appear/disappear on short timescales (Nespoli et al. 2003; Sriram et al. 2013). In this paper, we have made a detailed spectral-timing study of the transient type-B QPOs detected in three BHXBs. By comparing the spectra of the periods with and without the QPO, we find that the overall trend of the spectral ratio is very similar between sources. This similarity suggests that the transient QPOs in BHXBs might share the same physical origin.

As shown in the top panel of Fig. 8, the spectral ratio between BQ and NQ for each case is nearly constant or slight decreasing above 10 keV, and the value is significantly higher than unity. This means that the high-energy Comptonization emission is stronger when type-B QPOs appear. Liu et al. (2022b) found that the value above 10 keV is different between different cases in a source. In contrast, the total flux below 10 keV does not change too much. If the flux could be an indicator of mass accretion rate, our result implies that the appearance of type-B QPOs or not is not determined by the change of the global mass accretion rate only, given that the BQ/NQ transition can occur at different flux levels in an outburst (Zhang et al. 2021; Liu et al. 2022b).

At energies below 10 keV, the spectral change between BQ and NQ is more complex. We find that, in all cases, the Comptonization component flux increases whereas the disc component flux decreases from NQ to BQ. The flux change of the thermal component is inversely proportional to the flux change of the Comptonization component. This tight correlation supports the scenario proposed by Zhang et al. (2021) that the transient nature of the type-B QPO is associated with a redistribution of the accretion power between the disc and the Comptonization emission.

In MAXI J1348-630, Zhang et al. (2021) found that the type-B QPO only appears when the flux fraction of the Comptonization component is above a critical value. This threshold is also present here in GX 339-4. However, the critical value in GX 339-4 is inconsistent with that obtained in MAXI J1348-630, suggesting that source properties determine this critical value. The critical value may be related to the intrinsic parameters of the different BHXB systems (e.g., black hole mass, spin, inclination) or the different configurations of the accretion flow. The inclination of GX 339–4 is $36^{\circ} \pm 4^{\circ}$ (Ludlam et al. 2015) and the value is $36.5^{\circ} \pm 1^{\circ}$ for MAXI J1348–630 (Kumar et al. 2022). Therefore, it is less likely that inclination plays an important role in determining the critical value. GX 339-4 contains an extremely fast-spinning black hole with $a_* > 0.97$ (Ludlam et al. 2015), while MAXI J1348-630 has a moderately high spin $(a_* = 0.80 \pm 0.02,$ Kumar et al. 2022). The mass of GX 339–4 is not well constrained (2.3 $M_{\odot} < M_{BH} < 9.5 M_{\odot}$, Heida et al. 2017), whereas the mass of MAXI J1348–630 is $M_{\rm BH}$ = 8.7 ± 0.3 M_{\odot} (Kumar et al. 2022). Given the current measurements of the intrinsic parameters of the two systems, it is difficult to distinguish whether black hole mass or spin value determines the threshold.

The type-B QPO observed in the 2021 outburst of GX 339-4 was also studied by Peirano et al. (2023) using NICER and AstroSat data. They found that the rms and lag spectra of the type-B QPO in GX 339-4 are similar to those in MAXI J1348-630 (García et al. 2021a). In addition, by fitting the rms and lag spectra of the QPO with a time-dependent Comptonization model (Bellavita et al. 2022), these authors found that two physically-connected Comptonization components are needed to explain the radiative properties of the QPO: a small corona (~ $25R_g$) with a high feedback fraction of photons returning from the corona to the disc and a large corona $(\sim 1500R_g)$ with almost no feedback (Peirano et al. 2023). The small corona would be a compact region located close to the black hole, while the large corona would be a vertically extended region that may be the base of a relativistic jet or outflow. This supports our above finding that the increased hard component is not the only contributor to the modulation of the QPO flux.

4.2 Transitions between the PDS with type-B QPOs and strong broadband noise

Fast transitions between the PDS with type-B QPOs and strong broadband noise (BQ/BLN) are usually observed during the HIMS-SIMS state transition (e.g., Motta et al. 2011; Homan et al. 2020; Zhang et al. 2020b). Sometimes, a significant type-C QPO is detected when the broadband noise dominates. We found that the spectral ratio of this type of transition is significantly different from that of the BQ/NQ transition. As shown in the bottom panel of Fig. 8, the ratio shows a maximum at around 4 keV. Above 4 keV, the ratio decreases gradually with photon energy, changing from above unity to below unity at around 10 keV. We note that the decreasing trend is steeper below 10 keV. In addition, the different relation between thermal and Comptonization component flux during BLN/BQ transitions suggests that the physical process or the geometry leading to the two types of transitions is totally different.

In GX 339–4, we observed frequent BLN/BQ transitions during the period we study. Such phenomenon was also observed in the previous outbursts of GX 339–4 and in some other BHXBs (Belloni & Motta 2016). In addition, BQ/BLN transitions are also detected during the flip-flop variability. This corresponds to frequent state transitions between the HIMS and the SIMS. Nixon & Salvesen (2014) proposed a model to explain the state transitions in BHXBs considering the process of disc tearing. In this model, individual rings of gas in the disc break off and precess independently. The tearing of the disc and alignment with black hole spin can explain the frequent HIMS-SIMS transitions. However, this process happens on timescales of a few days (Nixon & Salvesen 2014). A previous study showed that the type-B QPO can appear/disappear within tens of seconds (Nespoli et al. 2003), contrary to the expectation of the above model.

Based on a systematic study of the reverberation lags in 10 BHXBs, including the three sources we studied in this work, Wang et al. (2022) found that the lags of the broadband noise component in the PDS become longer during the HIMS-SIMS state transition, suggesting that the corona is the base of the jet that vertically expands and/or is ejected during the transition. Zhang et al. (2022a) fitted simultaneously the time-averaged spectrum, the fractional rms and phase-lag spectra of the QPOs in MAXI J1535-571. The change of the geometry inferred from their results is that the corona expands vertically but contracts horizontally during the transition from the HIMS towards the SIMS. In this work, we find that the inner disk radius does not change too much from BLN to BQ. This also suggests that the spectral-timing evolution during the HIMS-SIMS state transition could be due to changes of the corona and/or geometry of the jet base. During the state transition from the HIMS to the SIMS, the jet properties change dramatically. The steady compact jet gradually switches off and relativistic discrete ejecta can be launched (e.g., Fender et al. 2009; Russell et al. 2019; Carotenuto et al. 2021). The evolution of the jet properties is also likely related to the change of the inner flow.

4.3 Possible changes in corona/jet geometry during the transitions

In the bright HS and the HIMS, type-C QPOs are usually present and accompanied by strong band-limited noise. The band-limited noise is supposed to originate from propagating fluctuations in mass accretion rate within a hot inner flow (Ingram 2016), and the type-C QPO can be produced by the global Lense-thirring precession of the same flow (Ingram et al. 2009). The change of the projection area of the hot flow along the line-of-sight leads to the flux modulation of the QPO. However, the type-C QPO becomes weaker or non-detectable at the end of the HIMS. In the form of the advection-dominated accretion flow (ADAF, Esin et al. 1997; Yuan & Narayan 2014), the gas cannot cool effectively and the accretion flow prefers a spherical accretion geometry (scale height $H/R \sim 1$). This symmetry becomes more dominant as the accretion rate increases in the outburst. Thus, the weakening of the type-C QPO could be due to the hot inner flow being very close to spherical so that the change of the projected area is minor, or the shrinking of the ADAF corona with increasing accretion rate. During the transition from BLN to BQ, the bandlimited noise component decreases significantly. From BLN to BQ, we find that the Comptonization component becomes softer and its flux decreases. Since the band-limited noise is usually related to the hot inner flow, we expect that the decrease of the band-limited noise is likely due to the shrinking of the hot flow region.

As mentioned earlier, the type-B QPO could be produced in the combined extended corona and the base of the jet. Liu et al. (2022b) proposed that the disappearance of the type-B QPO can be due to that the inner part of the flow becoming aligned with the black-hole spin axis due to the Bardeen-Petterson effect (Bardeen & Petterson 1975). From our spectral fitting, we find that the reflection fraction increases slightly when the type-B QPO disappears. The reflection fraction in the lamppost geometry is related to the corona height and the bulk velocity (You et al. 2021). Since we observe a constant lamp post height during the transitions (Table 3), the change of the reflection fraction.

5 CONCLUSIONS

We present a detailed spectral-timing analysis of the fast transitions of X-ray variability observed in the 2021 outburst of GX 339–4, and make a detailed comparison of the transitions between different black hole systems. The main results are:

(1) In the three black-hole X-ray binary systems GX 339–4, MAXI J1348–630 and MAXI J1820+070, the spectral ratios of BQ/BLN and BQ/NQ are very similar. The spectral ratio of BQ/NQ is nearly constant or slightly decreasing above 10 keV, but the value is different for each source. We also investigate the relative flux change of the thermal and Comptonization components during the appearance/disappearance of the type-B QPO and find a tight anti-correlation for the three sources with a slope ~-1 below 10 keV.

(2) Using a broadband spectral analysis, we find that the inner radius of the accretion disc shows no evident changes during the transitions. However, the spectrum becomes softer when the type-B QPO appears. When the type-B QPO disappears, the reflection fraction increases.

We suggest that a slightly truncated disc with a hot flow region exists in the BLN epoch and the hot flow region converts into a jet that might be precessing when the type-B QPO appears. The disappearance of the type-B QPO can be explained by a stop of the precession of the jet. During the appearance/disappearance of the type-B QPO, the redistribution of the accretion power between the disc and the jet plays a key role.

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Software: XSPEC (Arnaud 1996), Astropy (Astropy Collaboration et al. 2013), Numpy (van der Walt et al. 2011), Matplotlib (Hunter 2007), Stingray (Huppenkothen et al. 2019b,a).

DATA AVAILABILITY

The raw *NICER* data underlying this article are available in the HEASARC database. The raw *Insight*-HXMT data underlying this article are available at http://hxmten.ihep.ac.cn/.

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APPENDIX A: ADDITIONAL FIGURE

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Figure A1. *NICER* light curve (0.5–10 keV) (upper panels) and corresponding dynamical power spectra (lower panels) of GX 339–4 with a time resolution of 16s. We divide the light curves into four typical periods based on the properties of PDS: periods with type-B QPO (gray shaded), with strong band-limited noise (blue shaded), with flip-flop phenomenon (green shaded) and the period dominated by Poisson noise (magenta shaded).